



## Molecular Crystals and Liquid Crystals Incorporating Nonlinear Optics

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### Investigation of the Nematic-Isotropic Biphase in Thermotropic Main Chain Polymers. Homogeneity of the Pure Isotropic and Nematic Phases. Part III: NMR Study

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INVESTIGATION OF THE NEMATIC-ISOTROPIC BIPHASE IN  
THERMOTROPIC MAIN CHAIN POLYMERS. HOMOGENEITY OF THE  
PURE ISOTROPIC AND NEMATIC PHASES.  
PART III: NMR STUDY.

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Abstract Nematic fraction  $f_N$  and biphasic width are  
measured by combination of broad line PMR and DMR  
experiments and the data compared with microscopy and  
DSC results. Time dependence of  $f_N$  was monitored  
isothermally. Preliminary data suggest that:

- i) equilibrium distribution of chain lengths between  
I and N components is established rapidly;
- ii) supercooling at the I/N transition is of thermo-  
dynamic rather than kinetic origin. The DMR spectrum  
of PAA<sub>14</sub> is used to probe heterogeneity and  
isothermal evolution of molecular morphology in the  
pure N phase (model system of small molecules and  
polymers). Dynamics of homogenization of the N phase  
on the molecular level is extremely slow under normal  
laboratory conditions.

## INTRODUCTION

In the two preceding papers, polarizing microscopy<sup>1</sup> and  
DSC<sup>2</sup> were used to delineate the nematic-isotropic biphasic  
and to follow evolution of the gross morphology of main  
chain nematic polymers as a function of their thermal  
history in the precursor biphasic. For a given thermal  
history within the biphasic, homogeneity of chain length

distribution was also monitored upon isothermal annealing of the sample in either the pure N or pure I phase. Herein, we describe broad line NMR experiments designed to probe on a more molecular level some thermodynamic and kinetic aspects of phase segregation in these polymers.

We have previously used broad line NMR to delineate the N+I biphasic in DDA9 polymers<sup>3-4</sup>. The fraction of nematic component  $f_N$  at a given temperature was obtained by measuring the relative intensity under the narrow peak of the I component. NMR values of  $f_N$  and biphasic width are compared here with the corresponding data deduced from microscopy and DSC. NMR is further used to probe molecular morphology in the pure N phase and to observe a pre-transitional range of temperatures within the homogenized I phase. Upon isothermal annealing in the biphasic, macroscopic demixing of the I and N components and homogenization of their respective chain length distributions take place, as discussed previously. Microscopy and DSC provide a macroscopic approach to these processes, but offer no answer to the question of compositional equilibration within the biphasic (i.e. equilibration of chain length distribution between the I and N components, following the stage of orientational ordering). Here again, NMR is used to provide some elements of answer.

#### EXPERIMENTAL SECTION

Sample preparation, characterization and definitions of symbols used were as in Part I<sup>1</sup>. Twin model compounds deuterated on the spacer and 2,2'-dimethyl-4,4'-diacetoxyloxyazobenzene (Ac9Ac, a non mesomorphic analogue of the mesogen) were prepared as described in<sup>5</sup>. In the NMR experiments, the samples ( ~50-100mg of material) were

contained in standard 5mm tubes sealed under vacuum. The spectra were obtained using a CXP Bruker Spectrometer working of 90MHz for proton and a Bruker WM250 working at 38.4MHz for deuterium. The values of  $f_N$  were deduced by integration of the sharp line of the isotropic component as previously described<sup>3-4</sup>.

## RESULTS AND DISCUSSION

### TEMPERATURE DEPENDENCE AND ISOTHERMAL EVOLUTION OF $F_N$

In part II, temperature dependence of nematic fraction  $f_N$  was deduced from the relative enthalpy change associated with the nematic component and measured isothermally  $[(f_N)^{DSC}_{iso}]$  or by means of dynamic scans following complete demixing of the I and N components  $[(f_N)^{DSC}_{eq}]$ . These results are discussed more fully here in light of a comparison with  $f_N$  values measured by NMR. On Fig. 1 are plotted the values of  $f_N$  measured for polymer DDA9M5,200 under three different conditions of thermal history. When the sample is cooled from a well homogenized I phase, results are identical within experimental accuracy, with biphasic starting at 141°C. The data points plotted on heating a solid sample brutally placed in the middle of the biphasic 133°C illustrate the importance of thermal history on the values of  $f_N$ . The biphasic recorded on heating extends beyond the temperature range on cooling. Similar supercooling was observed by comparing  $(f_N)^{DSC}_{iso}$  and  $(f_N)^{DSC}_{eq}$  (Table III of ref. 2). Note that such supercooling is observed on cooling well homogenized samples.

Supercooling in well homogenized samples does not appear to be of kinetic origin: area of the isotropic peak recorded on cooling with thermal history of Fig. 1 was followed isothermally for 24 hours at 141°C ( $f_N$  on cooling

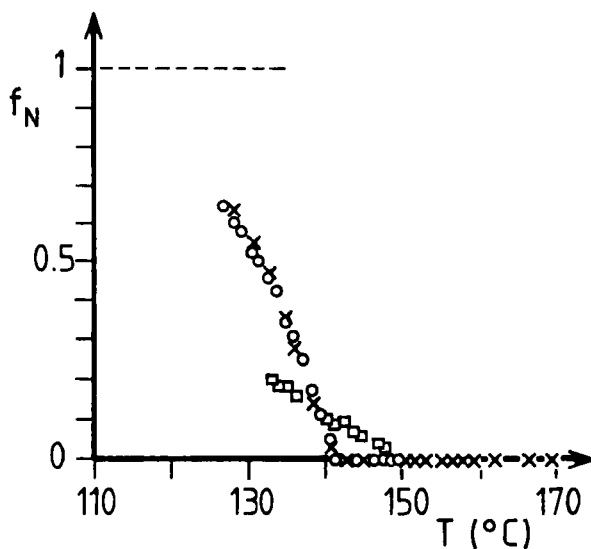


FIGURE 1.  $(f_N)_{\text{PMR}}$  for sample DDA9M5,200.

○ Isotropization for 3 hours at 150°C, followed by programmed cooling with 500'' between points.

× Isotropization for 45' at 170°C followed by the same cooling. □ Solid sample brutally placed in the N+I biphase at 133°C. Equilibration for 6 minutes. Data on heating with 120'' between points.

=0) and 138°C ( $f_N$  on cooling = 0.17) and remained constant over the time of the experiment.

On Fig. 2 are plotted the values of  $(f_N)_{\text{PMR}}$  and  $(f_N)_{\text{DMR}}$  measured on a 90/10(w/w) mixture of polymer DDA9M5,200 and twin model 9DDA9-d20 (deuterated on the spacer). Nematic fraction values were measured independently by PMR and DMR on cooling from a well isotropized I phase, as described in<sup>4</sup>. Kinetics of phase separation and reproducibility of points were checked by PMR (polymer) and DMR (model

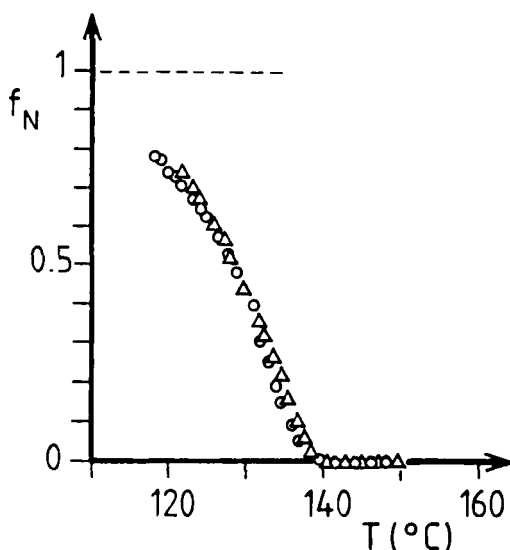


FIGURE 2.  $(f_N)_{\text{PMR}}$  ( $\circ$ ) and  $(f_N)_{\text{DMR}}$  ( $\triangle$ ) for a 90/10 (w/w) mixture of DDA9M5,200 and model 9DDA9-d20. Same thermal history in both PMR and DMR runs: isotropization for 3 hours at 150°C; 500" between points.

compound) as follows: i. DMR. Following equilibration in the I phase, the sample was cooled in less than a minute to 130°C and  $f_N$  followed isothermally for 24 hours with 200" between points. Value of  $f_N$  stabilized within one minute at the value measured on cooling with thermal history of fig. 1 ( $f_N \approx 0.44$ ) and did not change subsequently with time. ii. PMR Starting from 125°C ( $f_N \approx 0.63$ ), the sample was rapidly heated to 136°C ( $f_N \approx 0.25$ ) and again followed isothermally for 24 hours, with 20" between spectra. The value  $f_N = 0.25$  was recovered after 2' and remained unchanged. Note that agreement between  $f_N$  value on heating and cooling in this specific instance may be due to the limited range of

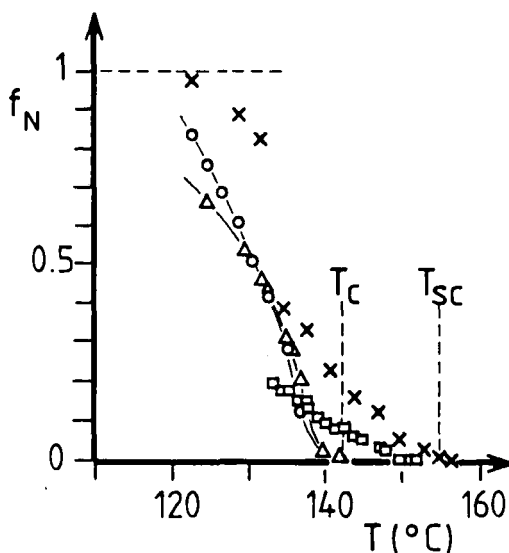


FIGURE 3. Comparison of  $f_N$  values (DDA9M5,200) derived from isothermal DSC ( $\circ$ ), dynamic DSC ( $\times$ ) and PMR (cooling ( $\triangle$ ) or heating ( $\square$ ) as on fig. 1).

thermal cycling within the biphasic ( $f_N=0.63-0.25$ ). However, all isothermal runs clearly show that compositional equilibration (i.e. equilibrium distribution of chain lengths between the I and N components of the biphasic) appears to occur in less than 1-2 minutes, which is the time required for stabilization of instrument response.

On fig. 3 are collected the values for temperature dependence of  $(f_N)_{\text{PMR}}$ ,  $(f_N)_{\text{iso}}^{\text{DSC}}$  and  $(f_N)_{\text{eq}}^{\text{DSC}}$  for DDA9M5,200, the last two measured as shown in the previous paper. Both  $(f_N)_{\text{PMR}}$  and  $(f_N)_{\text{iso}}^{\text{DSC}}$  were measured on cooling from a well isotropized I phase, whereas  $(f_N)_{\text{eq}}^{\text{DSC}}$  was obtained from cooling scans immediately following heating the demixed solid phase (see Table III in ref. 2). Note that sample



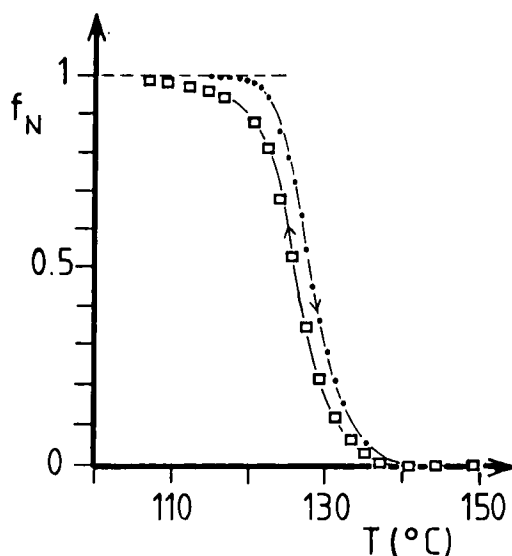


FIGURE 4. Comparison of  $f_N$  measured on heating and cooling through the biphas (DDA9M2,600). □; Cooling from a well isotropized I phase (1620" between points; ●; followed by heating from 105° (1000" between points).

DDA9M5,200 displays a biphas by microscopy until  $T_{sc}$ . To further illustrate influence of thermal history, sample DDA9M2,600 was isotropized at 150°C then cooled at 25°/min to 115°C, at the lower limit of the biphas. Following overnight annealing at 115°C,  $f_N$  was measured on heating. The values of  $f_N$  on heating were slightly shifted relative to  $f_N$  measured on cooling as shown on fig. 4.

Discrepancies between  $f_N$  on heating and  $f_N$  on cooling (from a well isotropized state) can be easily understood by considering molecular segregation processes. On heating, the longest molecules progressively concentrate in the remaining N phase and isotropize near their equilibrium

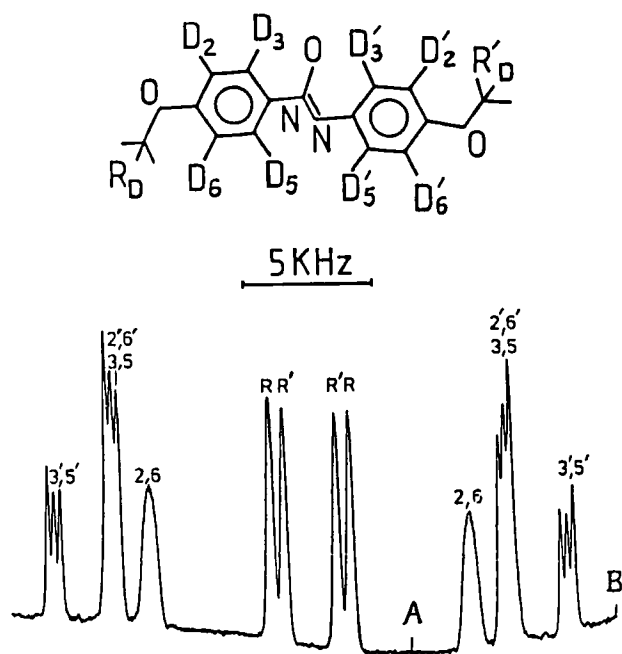


FIGURE 5. Typical DMR spectrum of neat PAAd14 in the N phase (peak assignments as <sup>15</sup>). The high field portion of the spectrum between A and B is used to probe homogeneity of the mixtures.

N/I transition temperature. On cooling (from a well isotropized I phase), the longest molecules are more molecularly dispersed and diluted with short chains. It is interesting to observe that  $f_N$  measured on cooling under such conditions does not change with time (over a span of 24 hours), as mentioned above. This might mean that supercooling, as illustrated on fig. 7 of ref.<sup>2</sup>, is inherent to the nature of the I/N transition in these systems. The temperature range  $T_c - T_{sc}$  (Fig. 3) can thus be considered as a pretransitional region where fluctuations of chain

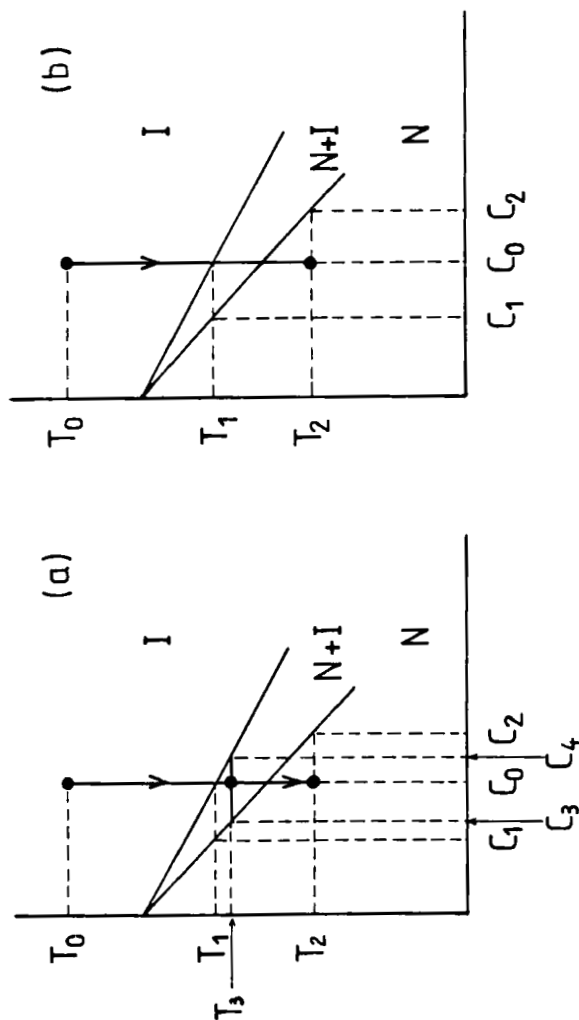


FIGURE 6. Thermal history of 85/15 (w/w) mixtures of PAA14-Ac9Ac shown on the phase diagram; a) Isotropization at  $T_0 = 152^\circ\text{C}$  for 10 minutes. Annealing for 24 hours at  $T_3 = 111^\circ\text{C}$ , roughly in the middle of the biphasic. Cooling to  $T_2 = 103^\circ\text{C}$ , in the pure N phase; b) Cooling from  $T_0$  to  $T_2$  at  $25^\circ\text{C}/\text{min}$ .

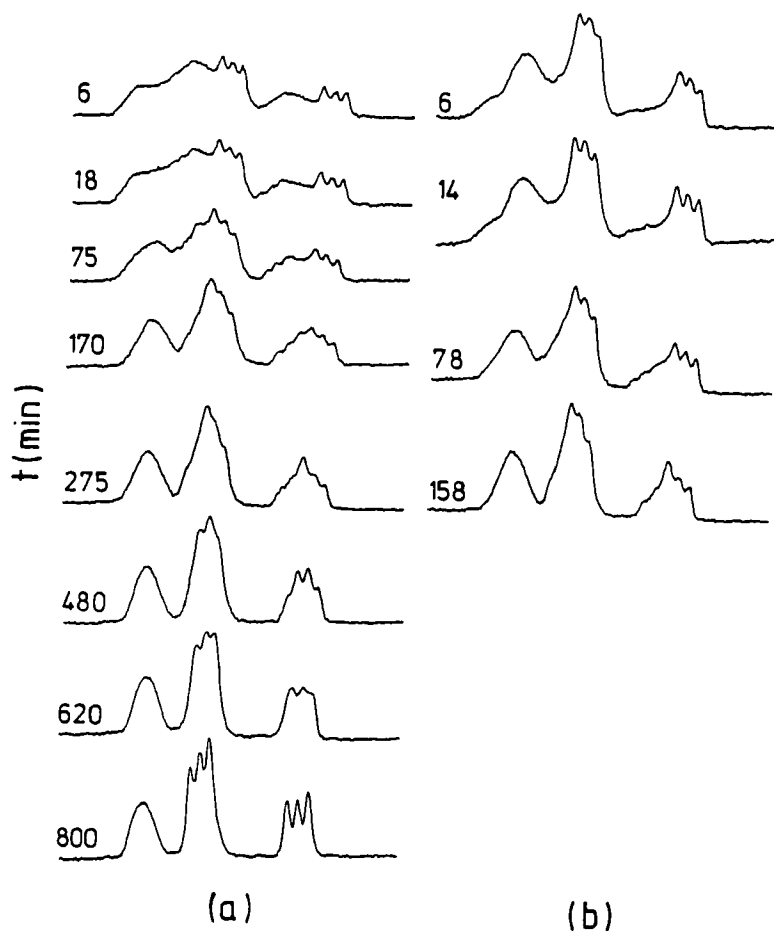


FIGURE 7a and b. Time dependence of the high field part of the DMR spectrum of PAAd14 in 85/15 (w/w) mixtures of PAAd14-Ac9Ac at 103°C. Time in minutes, thermal history corresponding to fig. 6a and b.

length distribution alone are unable to nucleate a nematic phase, starting from a reasonably homogeneous medium.

Our experiments provide no information concerning the dynamics of phase separation during the stage of

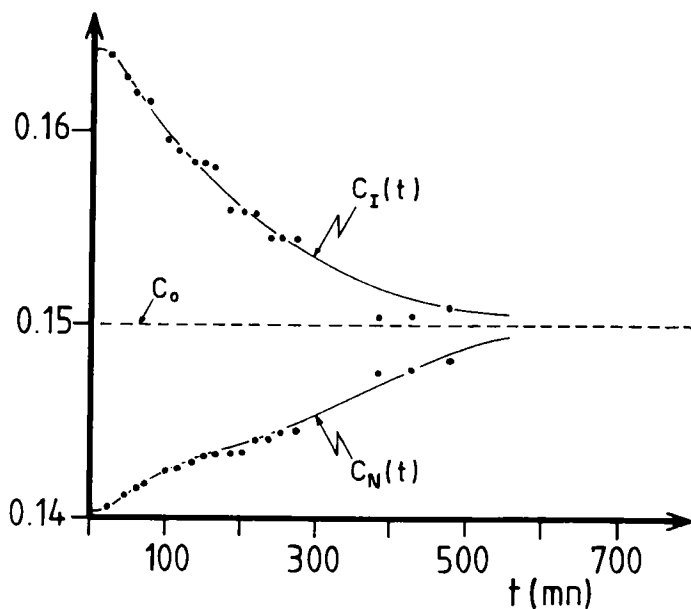


FIGURE 8. Time dependence of the mean concentrations  $c_N(t)$  and  $c_I(t)$  of Ac9Ac in FN and FI components homogenizing at temperature  $T_2=103^\circ\text{C}$  (thermal history as in 6a).

orientational and conformational ordering, such as would be obtainable from time-resolved SALS scans, for example. But they do illustrate the absence of appreciable net migration of chains across I/N boundaries following initial ordering. Macroscopic demixing between the I and N components occurs without measurable change in the value of  $f_N$ .

#### HOMOGENEITY OF THE NEMATIC PHASE: ISOTHERMAL EVOLUTION OF MOLECULAR MORPHOLOGY

Below  $T_c$ , nematic droplets grow through a process of molecular segregation. As a result, inhomogeneity in

chain length distribution will necessarily follow as the remaining I phase is progressively depleted of the longest chains. During isothermal annealing in the biphasic, chain length distribution will homogenize within the demixed I and N components via a process of diffusion. This homogenization is reflected in the progressive disappearance of the boundary region of intermediate chain lengths observed by microscopy upon demixing<sup>1</sup> and of the intermediate isotropization peak observed by DSC<sup>2</sup>. In order to follow this homogenization process on a more molecular level, we have carried out NMR experiments on a model system of low mass molecules and on various polymer samples.

#### Model System

Binary mixtures of nematic perdeuterated p-azoxyanisole (PAA<sub>d</sub>14) and 2,2'-dimethyl-4,4'-diacetoxyloxyazoxybenzene (Ac9Ac, a potentially nematic molecule comprising the mesogenic core of the polymer) were previously investigated<sup>6</sup>. The phase diagram was established. Order parameters of both components were measured independently through combination of DMR and PMR. In the present study, the DMR spectrum of PAA<sub>d</sub>14 was used as a probe and is illustrated on fig. 5. Note the well resolved and well separated lines. Triplet 3'5' was used to follow the distribution of concentration within the sample. Indeed, in<sup>6</sup> it was shown that, for each concentration and temperature, the position of this triplet is perfectly determined. Conversely, observation of distribution of positions at a fixed temperature necessarily reflects inhomogeneity of concentration.

Figures 6 and 7 schematize the experiments performed on a 85/15 (w/w) mixture of PAA<sub>d</sub>14-Ac9Ac. Experimental details are outlined in<sup>6</sup>. Thermal history of the

samples is summarized on figures 6a and b. On figures 7a and b is shown the time dependence of the high field part of the DMR spectrum of PAA<sub>dl4</sub> in the pure N phase at 103°C, with thermal history corresponding to 6a and b, respectively. Initial spectrum 7b is observed as the superposition of a reasonably well resolved triplet and a broad peak centered at lower frequencies. Initial spectrum 7a is similar but the lower frequency peak is significantly broader.

Initial spectra 7a and b can be explained as follows. At temperature  $T=T_1$  nematic droplets are nucleated with an average concentration  $c_1$ . The homogenization time of these droplets is diffusion controlled and proportional to their radius  $R(t)$ , with

$$\tau_{\text{hom}}(t) = \frac{R^2(t)}{6D} \quad (1)$$

( $D$ =Self diffusion coefficient).

As cooling proceeds along pathway 6b, these droplets grow from an isotropic phase that becomes progressively depleted in PAA. As long as  $\tau^{-1}(t)$  remains inferior to the cooling rate the droplets homogenize and the resulting portion of the N phase appears as a relatively well resolved triplet. The broad distribution of frequencies, then, corresponds to the remaining portion of the N phase and is centered at lower frequencies, as its average concentration in PAA is lower.

Along 6a, cooling starts from a macroscopically demixed N+I biphasic in which the concentrations of the two components have been homogenized, with concentrations  $c_3$  and  $c_4$  for components N and I respectively. Cooling to point  $T_2$  in the pure N phase results in a triplet

corresponding to the FN component (concentration  $c_3$ ) and a relatively broad distribution of frequencies (compared to case b) corresponding to FI.

Figures 7a and b roughly illustrate a metastable nematic  $N_1+N_2$  biphasic. The dynamics of its isothermal evolution provide a model for rationalization of phenomena observed in the case of polymers. On figure 8 is shown the time dependence of the mean concentration of Ac9Ac in FN and FI components during homogenization at temperature  $T_2=103^\circ\text{C}$ , following the evolution illustrated on figure 6a. The two concentrations tend toward their common equilibrium value in nearly exponential fashion. A mean homogenization time  $\tau_{1/2}$  may be defined as the time at which the deviation from equilibrium concentration is divided by two ( $\frac{1}{2}[c(o)-c_o]$ ). This time is of the order of 200 minutes and is compatible with a diffusion controlled homogenization of a macroscopically demixed system. Applying eq.1 with  $R\sim 3.5\text{mm}$  (average radius of the sample in the NMR tube) leads to a diffusion coefficient  $D\sim 2\times 10^{-6}\text{cm}^2\text{sec}^{-1}$ , in agreement with literature value of the self diffusion coefficient in nematic PAA at  $103^\circ\text{C}$ <sup>7</sup>.

Remixing of components and homogenization of concentration are slow even after a rapid cooling (figure 7b): compare spectrum at 275min in figure 7a with spectrum obtained at 158min. in fig. 7b. Clearly, such molecular homogenization will be orders of magnitude slower in the case of polymers. Since  $D\propto \gamma^{-1}$  (where  $\gamma$  is an average viscosity) and  $\tau_{1/2}\propto D^{-1}$ , homogenization times are expected to be proportional to the average viscosity of the medium. In the case of our polymer this viscosity is about 5 to 8 orders of magnitude higher than in PAA<sup>8-13</sup>.



### Polymers

Save for kinetics of homogenization, polymers are treated by exact analogy with the model system, provided the concentration gradient formed upon crossing the phase diagram is replaced with a gradient of chain length distribution. Due to molecular segregation, nematic droplets of polymer will grow by successive addition of roughly concentric shells of shorter and shorter average chain length. As a biphasic region must inevitably be crossed to reach a pure N phase, on heating or cooling, the nematic phase must inevitably segregate into metastable domains. Morphology of the N phase, and of the resulting solid, will depend on thermal history. Progressive homogenization of chain length distribution may be revealed as a time dependent rheological behavior upon isothermal aging of the mesophase. Evolution of optical textures from dense disclination lines to loosely threaded textures has been reported by several authors<sup>14</sup> and may perhaps be the result of such a homogenization.

Molecular homogeneity and dynamics of remixing in the pure N phase of polymer were tracked by following the DMR spectrum of PAA<sub>14</sub> dissolved at low concentration in AZA9 or DDA9, and acting as a probe. On fig. 9a and b is shown the time evolution of the spectrum of PAA<sub>14</sub> in AZA9 polymer, following thermal history corresponding to 6a and 6b. Two fractions ( $\frac{\overline{M}_w}{\overline{M}_n} \leq 1.1$ ) of mass 7,300 and 3,100 were mixed with PAA<sub>14</sub> in ratios 45/45/10 (w/w). Initial peak 9a, roughly a superposition of two peaks corresponding to FN and FI components, is slightly narrower after 3 hours, but the system is far from homogeneity. Initial spectrum 9b represents a more homogeneous morphology which evolves slowly, as illustrated by the progressive appearance of a

triplet. This triplet is still far from being well resolved after 60 hours.

By comparing time scale of homogenization and viscosity of polymer (fig. 9b) and model system (fig. 7b), one can estimate an order of magnitude for the dimensional scale of heterogeneity in this system. Taking a ratio of  $\sim 10^6$  between viscosities and  $\sim 30$  between time scales an average value  $\rho \sim 20 \mu$  is estimated.

On fig. 10 is shown the spectrum of PAAD14 in DDA9M4,000 (10/90 mixture) as the sample is heated from 118°C (pure N phase) to 146°C in the pure I phase. Thermal history corresponds to fig. 6a. The spectrum at 118°C appears as a superposition of a triplet corresponding to the FN component and a broad peak corresponding to the FI component. Peak separation is more pronounced than in AZA9 since concentration gradients are larger, due to an intrinsically larger biphasic gap, as discussed in<sup>1</sup>.

No evolution was observed at 118°C (over a period of 24 hours). Evolution of the spectrum during isotropization accurately reflects previous microscopic observation, namely sequential isotropization of the peaks corresponding to FI and FN components. The area corresponding to the triplet of the FN component remains constant between 118 and 127°C, i.e. until disappearance of the broad FI peak.

#### SUMMARY

The nematic phase of main chain PLCs is composed of metastable domains that result from molecular segregation by chain length, on heating and cooling. Thermal history in the precursor N+I biphasic determines the initial morphology of the resulting I or N phase. Dynamics of

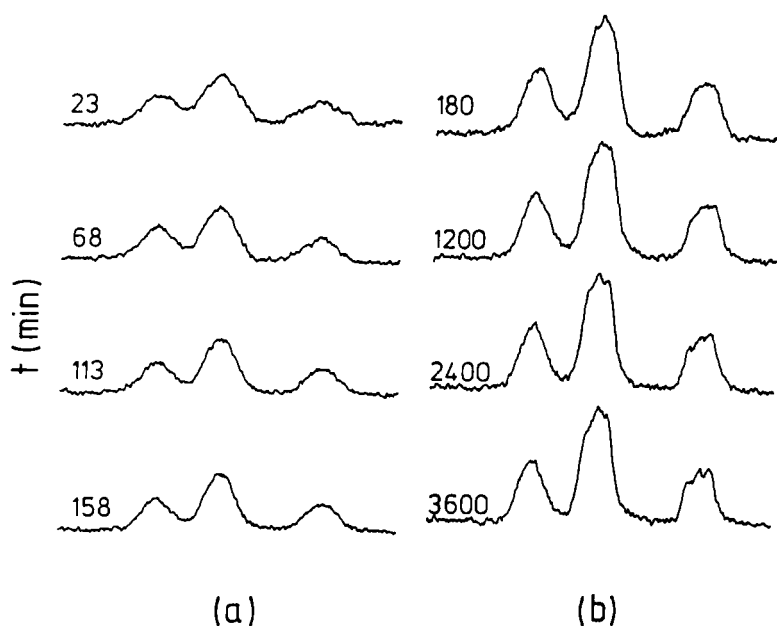


FIGURE 9. Time dependence of the high field portion of the DMR spectrum of PAAd14 in AZA9. Thermal history: a) Isotropization at 151°C for 3 hours; annealing 4.5 hours at 133°C, roughly in the middle of the biphasic; cooling to 115°C in 2 min. b) Isotropization at 151°C followed by cooling to 115°C in 2 min.

homogenization of the N phase on the molecular level is extremely slow on the time scale of normal laboratory conditions.

Juxtaposition of microscopy, DSC and NMR experiments provides a reasonable correlation between macroscopic and molecular interpretation of data. Save for time scale of events, kinetics of homogenization can be treated by exact analogy with a model system of small molecules in which

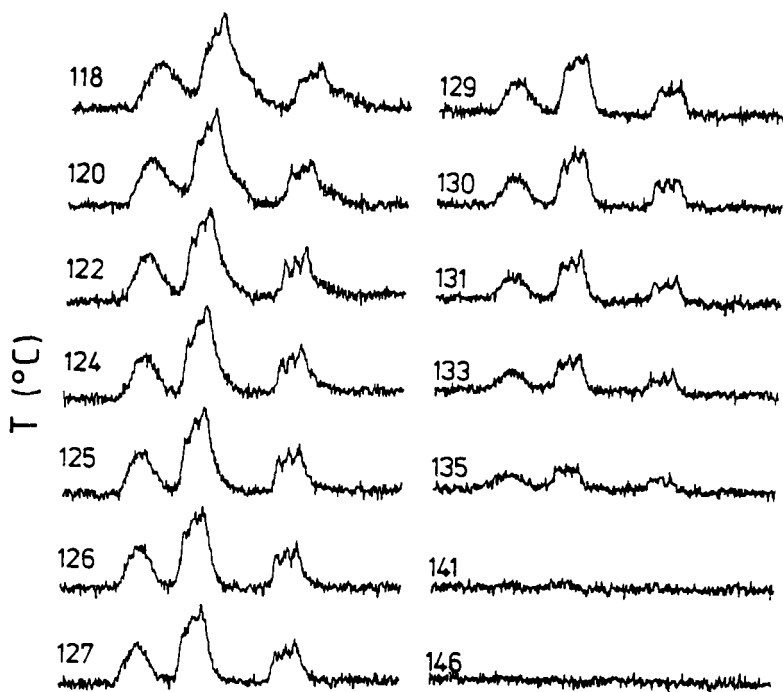


FIGURE 10. Evolution of the DMR spectrum of PAAd14 in DDA9M4,000 (10/90) during isotropization. Thermal history: isotropization at 150°C for 1.5 hours; annealing 14 hours at 131.5°C, roughly in the middle of the biphasic; cooling to 118°C in the pure N phase, followed by heating to 146°C, with 100 min. between spectra.

the phase diagram and molecular morphology were investigated by combination of DMR and PMR spectroscopy.

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